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1. MPS Model

i = product

k = semi-product

 c_{it} = penalty unit shortage cost of product i in week t

hit = penalty unit holding cost of product i in week t

<u>Sets</u>

j = line

Parameters [Varameters]

t = week

 D_{it} = demand of product i in week t

bi= beginning inventory of product i

vskj = velocity of semi-product k in line j

setupskj = setup of semi-product k in line j

minenvi= minimum inventory of product i

 α = importance weight for shortage cost $\gamma = \text{importance weight for holding cost}$

M = very large number

Sets

s= stage

j = line

<u>Parameters</u>

n = order

i, k = product

MPQ_i= minimum production quantity of product i

 w_{ij} = if product i can produce in line j 1, otherwise 0

maxi_{it} = maximum available hour of line j at week t

wskj= if semi-product k can produce in line j 1, otherwise 0

 r_{ki} = if semi-product k is a semi-product of product i 1, otherwise 0

workerij = number of workers required in line j to produce product i

workerki = number of workers required in line j to produce semi-product k

2. Flow Shop Scheduling (Non-Inline)

- = = = = = =

setup_{ij}= setup of product i in line j

v_{ij} = velocity of product i in line j

ETI GIDA Chocolate Factory Production Planning Optimization Project Ahmet Tok / Günce Demirtaş / Mine Sude Pinar / Rabia Hicran Örengül / Seda Sarmaz



INTRODUCTION

Eti Gıda was founded in Eskişehir in 1962 by Firuz Kanatlı.

The company produces biscuits, cookies, cakes, pies, chocolate, wafers, baby food and ready-made food products.

The project is carried out at Eskişehir Eti Chocolate Factory.



CURRENT SYSTEM

Production continues 24 hours a day in 3 shifts. Weekly and daily schedules are created to plan the production of products. There are 28 production lines in the factory. The capacities and speeds of lines different. The chocolate groups that can be produced on these lines may differ from each other. Set-up time between product groups are different. Sales of products are divided into three categories: international, export and local market. Products have different delivery priorities. A maximum stock period of 6-7 days is expected for the local market. Stock is not required for export and international products. Deliveries are made weekly.

PROBLEM DEFINITION

The main problem of the project is non-optimized production planning. The main reason for this is manual planning.

Since there is demand for finished products, a production plan is made according to the finished product. Therefore, the plan of semi-finished products is ignored. For this reason, problems such as overstocking, out-of-stock or shortage are occurring.

The firm needs a system that provides optimized planning by eliminating human-related planning errors to meet incoming demands.

Main Aim: Minimizing the cost and completion time

RESULT

The outputs of the MPS Model show how many kg of products should be produced in which week.

|| Flow Shop Scheduling Model shows the products to be produced in non-inline production should be produced on which line, in which order and for how long. Parallel Machine Scheduling Model shows the products produced in inline produc-It ion should be produced on which line in which order and for how long.





METHODOLOGY



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z_i = production amount of product i
v_{ij} = velocity of product i in line j
w_{isj} = if product i can produce on stage s in line j 1, otherwise 0
$setup_{ij}$ = setup time of product i in line j
sp_{ij} = waiting time of product i in line j

WEEKLY SCHEDULING

· 6-Day (1 week) Scheduling

Constraints

∀i,t

∀i,t

 $\forall i, t > 1$

∀j,t

∀j,t

∀i,j,t

∀i,j,t

∀k,j,t

∀i,j,t

 $\forall i, t > 1$

∀k,t

∀t

∀t

∀i,t

∀k,t

(4)

(6)

(7)

(11)

(12)

(13)

(14)

(15)

(17)

(18)

(20)

(1)

(2)

(3)

(10)

(11)

Decision	Variables

$a_{ijt} = \text{if product } i \text{ was assigned to line } j \text{ at week t } 1, \text{ otherwise } 0$		$I_{it}^{-} = \sum z_{ijt} + I_{it}^{+} - D_{it}$
as_{kjt} = if semi-product k was assigned to line j at week t 1, otherwise 0		$l^{\pm}_{ij} = h_i$
$zresult_{it} = production$ quantity of product i week t		$t_{11}^{\dagger} = b_1$
z_{ijt} = production quantity of product i in line j at week t		$I_{it+1} = I_{it} + \sum_{j} I_{jt} = D_{it}$
$zsresult_{kt} =$ production quantity of semi-product k at week t		$\sum_{i} z_{ijt} v_{ij} + \sum_{i} a_{ijt} setup_{ij} \le maxi_{jt}$
zs_{kjt} = production quantity of semi-product k in line j at week t		$\sum_{zs_{kjt}vs_{kj}} + \sum_{as_{kjt}setups_{kj}} \le maxi_{jt}$
I_{it}^+ = amount of on hand inventory of product i in week t		$\underline{\Box}_k \leq \underline{\Box}_k$ $Z_{iilet} \leq Ma_{iit}$
I_{it}^- = amount of shortage of product i in week t		$a_{ijt} \leq w_{ij}$
Formulation		$as_{kjt} \leq ws_{kj}$
Objective Function		$z_{ijt} \ge MPQ_i a_{ijt}$
Minimization of the cost is the objective of this model. The cost is the summation of total hold	ling	$minenv_i \leq I_{it}^+$
cost and total holding cost in equation 1.		$\sum z_{s_{kjt}} \geq \sum z_{ijt} r_{ki}$
$Min TC = \alpha SC + \gamma HC$	(1)	$\Delta_j = \Delta_{ij}$
Objective Function Elements		$\sum_{i,j} a_{ijt} worker_{ij} \le 6145$
$SC = \sum_{it} c_{it} I_{it}^{-}$	(2)	$\sum_{i,j} a_{ijt} workers_{kj} \le 950$
Shortage cost is a multiplication of the unit penalty shortage cost of product i in week t and	the	$\sum_{n=1}^{\infty} \pi_{n} = \pi_{n} = \pi_{n}$
amount of shortage of product i at week t.		$\sum_{j} z_{ijt} = z_{i} esalut$
$HC = \sum_{it} h_{it} I_{it}^+$	(3)	$\sum_{j} zs_{ijt} = zsresult_{kt}$
Holding cost is a multiplication of the unit penalty holding cost of product i in week t and	the	$a_{ijt}, as_{kjt} \in \{0,1\}$
amount of on hand inventory of product i at week t.		$z_{ijt}, zs_{kjt}, HC, I_{it}^+ \ge 0$

3. Parallel Machine Scheduling

<u>Sets</u> i, k = productj = linen = order**Parameters** $time_{ij}$ = processing time of product i line j

 $setup_{ii}$ = setup time of product i in line j

 w_{ij} = if product i can produce in line j 1, otherwise 0

M = Big M (a sufficiently large number)





Product No	duct No Required		ті	Project	
2	1451	1451		1451	
5	1222	750 2651 4320 750 0 10604 0 0		1568	
6	2651			2651	
407	4320			4320	
408	457			750	
411	0			0	
582	10604			10604	
584	0			0	
604	0			0	
Cost of ETI	Cost of Proj	Cost of Project			
86350	75315 243	9		12 78%	

INTERFACE



M = Big M (a sufficiently large number)

Decision Variables

 C_{isj} = completion time of product i at stage s in line j

Cmaxi = maximum completion time

 x_{isjn} = if product is assigned to stage s line j at order n 1, otherwise 0

Formulation			
Objective Function			
Min Z = Cmaxi			
Constraints			
$\sum_{jn} x_{isjn} = 1$	∀i,s	1	(1)
$x_{isjn} \leq w_{isj}$	∀i,s,	j,n	(2)
$\sum_{i} x_{isjn} \leq 1$	∀s,j	j,n	(3)
$c_{i2j} + M(1 - x_{i2j1}) \ge c_{i1j} + v_{ij}z_i + sp_{ij}$	∀i	,j	(4)
$c_{isj} - c_{ksj} + M(2 - x_{isjn-1} - x_{ksjn}) \ge (v_{ij}z_i + setup_{ij}) + s_{ij}$	p _{ij}	$\forall j, i \neq k, n > 1, s$	(5)
$c_{i2j} \ge c_{i1j} + v_{ij}z_i + +sp_{ij}$		∀i,j	(6)
$Cmaxi \ge c_{isj}$		∀i,s,j	(7)
$\sum_{k} x_{ksjn} - \sum_{i} x_{isj(n-1)} \le 0$		$\forall s, j, n > 1$	(8)
$x_{isjn} \ \epsilon \left\{ 0,1 \right\}$			(9)
$c_{isj}, Cmaxi \ge 0$			(10)

Decision Variables C_{ij} = completion time of product i Cmaxi = maximum completion time $x_{ijn} =$ if product i is assigned to line j in order n 1, otherwise 0 a_i = starting time of product i

Objective Function	
Min Z = Cmaxi	
Constraints	
$\sum_{i} x_{ijn} \leq 1$	∀j, n
$\sum_{nj} x_{ijn} = 1$	$\forall i$
$\sum_{i} x_{ijn} - \sum_{k} x_{kj(n-1)} \le 0$	$\forall j, n > 1$
$c_{ij} + M(1 - x_{ij1}) \ge setup_{ij} + time_{ij}$	∀i,n,j
$c_{ij} + M(2 - x_{ijn} - x_{kjn-1}) \ge c_{kj} + setup_{ij} + time_{ij}$	$\forall j, i \neq k, n > 1$
$Cmaxi \ge c_{ij}$	$\forall i$
$w_{ij} \ge x_{ijn}$	∀i,j,n
$a_i \geq c_{ij} - M(2 - x_{ijn} - x_{ijn-1})$	$\forall i \neq k, j, n > 1$
$a_i \leq M(1-x_{ij1})$	$\forall i \neq k, j, n > 1$
$x_{ijn} \epsilon \{0,1\}$	
$c_i, Cmaxi \geq 0$	

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Ν	1PS and Scheduling models were developed us	sing GAMS for weekly plans.						
А	detailed 12-week production plan was develo	pped, taking into account product priori-						
ti	es and changeover times.							
S	Shortage and inventory costs are minimized by using restrictions on production lines							
2	and raw material stacks							
а т	hu law material stocks.							
I	ne interface has been developed for the comp	any's use.						
A	13% improvement in planning efficiency was	achieved.						
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-	References							
]1 [2	Afoakwa, E. O. (2016). "Industrial Chocolate Manufacture – Processes And Factors Influencing Quality". In Chocolate Al-Ashhab M.S., and Fadag H (2018). "Multi-Product Master Production Scheduling Optimization Modelling	Science and Technology (2nd ed.). Jsing Mixed Integer Linear Programming And Genetic Algorithms." International Journal of Research -						
Gi [3 [4	 ranthaalayah, 6(5), 78-92. Alavian, P., Denno, P., & Meerkov, S. M. (2017). "Multi-job production systems: Definition, problems, and produc Başar, R., & Engin, O. (2022). "Beklemesiz Akış Tipi Çizelgeleme Problemlerinin Analizi Ve Hibrit Dağınık Aram. 	-mix performance portrait of serial lines". International Journal of Production Research, 55(24), 1-26. Yöntemi lle Çözümü". Çanakkale Onsekiz Mart University Journal of Advanced Research in Natural and Applied						
Sc [5 [6 [7	 iences, vol8(2), pages 293-308 Berglund, M. & Karltun, J., (2007). "Human, Technological And Organizational Aspects Influencing The Produc Bilgen, B., & Doğan, K. (2015). "Multi-Stage Production Planning in The Dairy Industry: A Mixed Integer Linear Chung, CH., & Krajewski, L. J. (1984). "Planning Horizons For Master Production Scheduling". Journal of Ope Ciolous F. (2006). "Chocilate Production In Lines Scheduling: A Case Study" IM S Master of Science I Middle Ea 	tion Scheduling Process," International Journal of Production Economics, Elsevier, vol. 110(1-2), pages 160-174. Programming Approach." Industrial & Engineering Chemistry Research 2015 54 (46), 11709-11719. ations Management, 4(4).						
[9 6(2) Enami, S., Barzegara, F., & Divsalar, A. (2019). "A Mathematical Model for Production Planning and Scheduli 2), 1-16.	ig in a Production System: A Case Study." International Journal of Industrial Engineering & Management Science,						
[1 Sc [1	 Farizal, F., Gaoriel D.S., Rachman A. & Kinaldi I. (2021). "Production Scheduling Optimization to Minimize Makes ience and Engineering, v. 1041, n. 1, p. 012046. Graves, S.C. (1981). "A Review Of Production Scheduling". Operations Research, vol 29(4), pages 646-675. 	oan and the Number of Machines with Mixed integer Linear Programming." IOP Conference Series: Materials						
[1 [1 [1	 Gutiérrez, T. J. (2017). "State-Of-The-Art Chocolate Manufacture: A Review". Comprehensive Reviews in Food Sc. Işık, E. E., Yıldız, S. A., & Şatır, Ö., (2023). "Constraint Programming Models For The Hybrid Flow Shop Scheduling Koskela, L. & Ballard, G. & Howell, G. & Tommelein, I. (2002). "The Foundations Of Lean Construction". 	ence and Food Safety, vol 16, pages 1313-1344. Problem And Its Extensions". Soft Computing, vol.2023, 1-28. Construction: Building in Value.						
[1 51	5] Magatao, L., Polli, H., Relvas, S., & Barbosa-Povoa, A. (2012). "Planning And Sequencing Product Distribution In A , 4591–4609. 61. Malarha E. (2002). "Sectoral Systems Of Innovation And Production". Research Policy, vol. 31(2), pages 247-264.	Real-World Pipeline Network: An MILP Decomposition Approach. [®] Industrial & Engineering Chemistry Research,						
[1	 Maletoa, T. (2002). Sectoral Systems of minovation and Floudction. Research Forcy, vol. 51(2), pages 247-204. Ojstersek, R., Brezocnik, M., & Buchmeister, B. (202). "Multi-Objective Optimization Of Production Scheduling V (3):359–376. 	/ith Evolutionary Computation: A Review." International Journal of Industrial Engineering Computations,						
[1 A(b) rancey, S., Linin, W., Guru, S. M. and Buyya, K. (2010). "A Particle Swarm Optimization-Based Heuristic for Sched dvanced Information Networking and Applications, pp. 400-407 9) Sağır, M., & Okul, H. D. (2020). "Restricted Enumeration And Machine Grouping Based Approach For Hybrid Flexi	uning worknow Applications in Cloud Computing Environments," 2010 24th IEEE International Conterence on ble Flow Shop Scheduling Problems With Sequence-Dependent Setup Times". Endüstri Mühendisliği / Journal of						
In [2 [2	dustrial Engineering, vol 31(3), 337-352. 0] Seda, M. (2007). "Mathematical Models of Flow Shop and JobShop Scheduling Problems." World Academy of Sc 5) Apairo, Jeremy F. (1993). "Mathematical Programming Models And Methods For Production Planning And Sch	ence,Engineering and Technology.vol 1 (31), 122–127. duling". Handbooks in Operations Research and Management Science. Vol 4: 371–443.						
[2	 Soares, M.M. & Vieira, G.E. (2009) "A New Multi-Objective Optimization Method for Master Production Schedulin 	g Problems Based on Genetic Algorithm". International Journal Advanced Manufacturing Technology, 41, 549-567.						

